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A Study on Compressive Anisotropy and Nonassociated Flow Plasticity of the AZ31 Magnesium Alloy in Hot Rolling

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Effect of anisotropy in compression is studied on hot rolling of AZ31 magnesium alloy with a three-dimensional constitutive model based on the quadratic Hill48 yield criterion and nonassociated flow rule (non-AFR). The constitutive model is characterized by compressive tests of AZ31 billets since plastic deformations of materials are mostly caused by compression during rolling processes. The characterized plasticity model is implemented into ABAQUS/Explicit as a user-defined material subroutine (VUMAT) based on semi-implicit backward Euler’s method. The subroutine is employed to simulate square-bar rolling processes. The simulation results are compared with rolled specimens and those predicted by the von Mises and the Hill48 yield function under AFR. Moreover, strip rolling is also simulated for AZ31 with the Hill48 yield function under non-AFR. The strip rolling simulation demonstrates that the lateral spread generated by the non-AFR model is in good agreement with experimental data. These comparisons between simulation and experiments validate that the proposed Hill48 yield function under non-AFR provides satisfactory description of plastic deformation behavior in hot rolling for AZ31 alloys in case that the anisotropic parameters in the Hill48 yield function and the non-associated flow rule are calibrated by the compressive experimental results.

1. Introduction

Anisotropic mechanical characteristics of the AZ31 magnesium alloy have a significant influence on plastic deformation and should be considered carefully for accurate simulation of forming processes. For decades many researchers have focused on the anisotropic constitutive models of metallic sheets which are all rolled products, whereas rare anisotropic models are adopted in hot rolling simulations. Montmitonnet et al. [1] simulated the hot rolling processes of steels but did not present experimental validation. Massé et al. [2] studied the lateral spread of pearlitic steel flat wire in cold rolling and concluded that taking into account plastic anisotropy significantly improves the estimation of the final width. Except for reported results above, effect of anisotropy has not been comprehensively investigated during hot rolling processes especially for hot rolling of AZ31 magnesium alloys with strong effect of anisotropy.

The foundation of most anisotropic constitutive models has been based on the associated flow rule (AFR) hypothesis which states that the flow rule is associated with the yield criterion. In other words, the yield function is also the potential for plastic strain rate in AFR based models. Accordingly, starting from Hill’s quadratic anisotropy model [3], various yield functions have been proposed to describe the anisotropy of metallic sheets. A detailed review can be found in Mohsen Safaei’s doctoral dissertation [4]. More recently, strength-differential effect was extensively studied and modeled by several yield functions proposed, such as Cazacu and Barlat [5], Cazacu et al. [6], Lou et al. [7], and Yoon et al. [8].

Most yield functions proposed are coupled with AFR. However, various studies described the difficulty of the
AFR concept in dealing with highly anisotropic materials. For instance, Cvitanić et al. [9] showed that Hill 1948 and Karafillis-Boyce 1993 anisotropic yield functions cannot predict both directional \( R \)-values and yield stresses simultaneously for AA2008-T4 and AA2090-T3. Yoon et al. [10] showed that Hill 1948 is unable to predict the exact numbers of ears in deep drawn cups made of AA2090-T3. Park and Chung [11] reported that Hill 1948 and Yld2000-2d generate poor accuracy for directional \( R \)-values and yield stresses for AA2090-T3 and AA5042. Therefore it can be concluded that it is difficult to describe a highly anisotropic material in terms of both plastic strain rate and yielding behavior with an identical function for yielding criterion and plastic potential.

The nonassociated flow rule approach neglects the constraint of equality of plastic potential and yield function enforced by the AFR assumption and can be an alternative but efficient approach to improve the accuracy of anisotropic yield functions even though there are some disadvantages related to non-AFR, such as issues about stability and thermodynamic consistency. Accordingly, the yield function and plastic potential function are assumed to be independent and used to describe the elastic limit and plastic strain rate direction, respectively. This assumption leads to various advantages and flexibility such that a larger number of experimental data are used for calibration of the parameters of yield and plastic potential functions, which results in a better agreement between simulation and experimental data, for example, better prediction of yield stresses and Lankford coefficients (width to thickness plastic strain ratios) at multiple in-plane orientations. When \( R \)-values and yield stresses from a highly anisotropic material are fit to one function, large gradients in the curvature of that function may occur and result in numerical convergence problems. These numerical convergence problems are solved by the non-AFR approach because these nonphysical curvature gradients are reduced by non-AFR [12].

Stoughton [13] first accurately predicted the \( R \)-value distribution and uniaxial and biaxial yield behaviors based on a non-AFR Hill48 model. After that, the non-AFR based approach has attracted increasing attentions for metal plas-

2. Constitutive Model

2.1. Anisotropic Yield Function. The three-dimensional yield function proposed by Hill [3] is defined as

\[
f_y = F_y(\sigma_{22} - \sigma_{33})^2 + G_y(\sigma_{33} - \sigma_{11})^2 + H_y(\sigma_{11} - \sigma_{22})^2 + 2L_y\sigma_{23}^2 + 2M_y\sigma_{31}^2 + 2N_y\sigma_{12}^2 - \sigma_y^2,
\]

where \( F_y, G_y, H_y, L_y, M_y, N_y \) are used to describe the direction-dependent yield stresses. To calibrate these coefficients, consider a uniaxial compression at an angle \( \theta \) from the rolling direction and denote the uniaxial compressive yield stress \( \sigma_\theta \). The stress components in the Cartesian axis system (orthotropic axes 1, 2, and 3 with 1-axis in the rolling direction, 2-axis in the transverse direction, and 3-axis in the thickness direction) are

\[
\sigma_{11} = \sigma_\theta \cos^2 \theta, \quad \sigma_{22} = \sigma_\theta \sin^2 \theta, \quad \sigma_{12} = \sigma_\theta \sin \theta \cos \theta.
\]

The substitution of (2) into (1) provides

\[
\sigma_\theta = \left(1 - \left((F_y + H_y) \sin^2 \theta + (G_y + H_y) \cos^2 \theta - 2H_y \sin^2 \theta \cos^2 \theta + 2N_y \sin^2 \theta \cos^2 \theta \right)\right)^{1/2} \sigma_y.
\]
Specifically, the uniaxial compressive yield stresses are formulated for the rolling direction (0°), diagonal direction (45°), and transverse direction (90°) as follows:

\[
s_0 = \left(\frac{1}{G_y + H_y}\right)^{1/2} \bar{\sigma}_y, \tag{3.1}\n\]
\[
s_{45} = \left(\frac{4}{F_y + G_y + 2N_y}\right)^{1/2} \bar{\sigma}_y, \tag{3.2}\n\]
\[
s_{90} = \left(\frac{1}{F_y + H_y}\right)^{1/2} \bar{\sigma}_y. \tag{3.3}\n\]

The uniaxial compression yield stress in the vertical direction denoted as \(s_z\) can be easily expressed as below:

\[
s_z = \left(\frac{1}{F_y + G_y}\right)^{1/2} \bar{\sigma}_y. \tag{3.4}\n\]

Four anisotropic parameters are formulated by solving equations of (3.2) and (3.4) as follows:

\[
F_y = \frac{1}{2} \left(\frac{1}{s_0} - \frac{1}{s_{45}} + \frac{1}{s_z}\right) \bar{\sigma}_y^2, \tag{3.5}\n\]
\[
G_y = \frac{1}{2} \left(\frac{1}{s_0} - \frac{1}{s_{90}} + \frac{1}{s_z}\right) \bar{\sigma}_y^2, \tag{3.6}\n\]
\[
H_y = \frac{1}{2} \left(\frac{1}{s_{45}} - \frac{1}{s_0} - \frac{1}{s_z}\right) \bar{\sigma}_y^2, \tag{3.7}\n\]
\[
M_y = \frac{2}{(s_{45})^2} - \frac{1}{(s_z)^2} \bar{\sigma}_y^2. \tag{3.8}\n\]

The through-thickness shear-related anisotropic parameters \(L_y\) and \(M_y\) are assumed to be identical with the shear-related anisotropic parameter of \(N_y\) and calculated as below:

\[
L_y = M_y = N_y. \tag{3.9}\n\]

2.2. Nonassociated Flow Rule. Assuming isotropic linear elasticity and additive decomposition of the strain increment tensor \(d\varepsilon\) into elastic part \(d\varepsilon^e\) and plastic part \(d\varepsilon^p\), the stress increment tensor reads

\[
d\sigma = C^e : d\varepsilon^e = C^p : (d\varepsilon - d\varepsilon^p), \tag{4.1}\n\]

where \(d\sigma\) is the stress increment tensor, \(d\varepsilon\) is the total strain increment tensor, \(d\varepsilon^e\) is the elastic strain increment tensor, \(d\varepsilon^p\) is the plastic strain increment tensor, and \(C^e\) is the tensor of elastic moduli. In non-AFR based models, the two independent formulations of yield stress and plastic flow direction determine the yielding and directional plastic strain rate, respectively. The plastic flow direction is determined by the plastic potential \(f_p\) as below:

\[
d\varepsilon^p = d\lambda \frac{\partial f_p(s)}{\partial \sigma}, \tag{4.2}\n\]

The plastic potential function \(f_p\) is assumed to have a Hill48 form of

\[
f_p = F_p(s_{22} - s_{33})^2 + G_p(s_{33} - s_{11})^2 + H_p(s_{11} - s_{22})^2 + 2L_p s_{23}^2 + 2M_p s_{31}^2 + 2N_p s_{12}^2 - \bar{\sigma}_p^2. \tag{4.3}\n\]

Here \(f_p\) is a continuously differentiable function and \(d\lambda\) is a nonnegative scalar called plastic multiplier or consistency parameter. By partial derivatives, the specific plastic strain increments are derived:

\[
d\varepsilon^p_{11} = 2d\lambda \left[ H_p (s_{11} - s_{22}) - G_p (s_{33} - s_{11}) \right], \tag{4.4}\n\]
\[
d\varepsilon^p_{22} = 2d\lambda \left[ F_p (s_{22} - s_{33}) - H_p (s_{11} - s_{22}) \right], \tag{4.5}\n\]
\[
d\varepsilon^p_{33} = 2d\lambda \left[ G_p (s_{33} - s_{11}) - F_p (s_{22} - s_{33}) \right], \tag{4.6}\n\]
\[
d\varepsilon^p_{12} = d\varepsilon^p_{21} = 4d\lambda N_p \varepsilon_{12}, \tag{4.7}\n\]
\[
d\varepsilon^p_{23} = d\varepsilon^p_{32} = 4d\lambda L_p \varepsilon_{23}, \tag{4.8}\n\]
\[
d\varepsilon^p_{31} = d\varepsilon^p_{13} = 4d\lambda M_p \varepsilon_{31}. \tag{4.9}\n\]

For the sample compressed at the direction of \(\theta^\circ\) from the rolling direction, the Lankford coefficient is

\[
R_\theta = \frac{d\varepsilon_{\theta+90^\circ}}{d\varepsilon_{33}} = -\left( \frac{\partial f_p}{\partial \sigma_{11}} \sin^2 \theta + \frac{\partial f_p}{\partial \sigma_{22}} \cos^2 \theta \right)
\]
\[
- \frac{\partial f_p}{\partial \sigma_{12}} \sin \theta \cos \theta \times \left( \frac{\partial f_p}{\partial \sigma_{11}} + \frac{\partial f_p}{\partial \sigma_{22}} \right)^{-1} \tag{4.10}\n\]
\[
= \left( G_p + F_p \tan^2 \theta \sin^2 \theta + 2N_p \sin^2 \theta \right)
\]
\[
- \left( F_p + G_p + 3H_p \right) \sin^2 \theta \times \left( G_p + F_p \tan^2 \theta \right)^{-1}. \tag{4.11}\n\]

Based on the experimental data of \(R_0, R_{45}\) and \(R_{90}\) as well as the uniaxial compressive yield stress along the through-thickness direction of \(s_z\), the anisotropic parameters of the Hill48 plastic potential function are obtained:

\[
F_p = \frac{R_0}{(R_0 + R_{45}) s_z}, \quad G_p = \frac{R_{90}}{(R_0 + R_{90}) s_z^2}, \tag{4.12}\n\]
\[
H_p = \frac{R_p R_{90}}{(R_0 + R_{90}) s_z^2}, \quad N_p = \frac{2R_{45} + 1}{2s_z^2}. \tag{4.13}\n\]

The anisotropic parameters of \(L_y\) and \(M_y\) are assumed to be identical with the value of \(N_y\). It should be noticed that the difference between the stress-shaped yield function and \(R\)-value shaped plastic potential function of Hill 1948 is the type of experimental inputs for parameter identification.
3. Experiments

As the billet during hot rolling mainly experiences compressive loading, the compression tests are carried out to calibrate anisotropic parameters in the yield function and non-AFR potential function. The thickness of the original billet is 300 mm and reduces to 12 mm after fifteen rolling passes. The rolling temperature declines from the initial 370°C to 265°C. Specimens of 12 mm × 12 mm × 12 mm are machined and compressed along the planar directions of 0°, 30°, 45°, 60°, 90°, and the vertical direction, as illustrated in Figure 1. Specimens are heated up to 265°C and kept at this temperature for 5 minutes before specimens are tested. The specimens are compressed by the reduction of 40% at the speed of 0.5 mm/minute. Specimens after compression are calibrated by experimental stress-plastic strain curve from uniaxial compression test along the vertical direction.

The yield stresses and Lankford coefficients at different directions are measured and presented in Table 1. It is obvious that the compressive yield stress along the transverse direction is much larger than those along other directions, while the R-value of vertically compressed specimen is a little higher than the others. Then these experimental data in Table 1 are utilized to calibrate the anisotropic parameters in the yield function and plastic potential function of Hill48, respectively with (6)–(10) and (16). T herein the yield stress at the vertical direction is used to represent the effective yield stress in (1) and in (13). The anisotropic parameters calibrated are summarized in Tables 2 and 3.

The anisotropies in compressive yield stresses and R-values by the AFR and non-AFR Hill48 models are predicted and compared with experimental results in Figures 3 and 4, respectively. The results demonstrate that the proposed non-AFR Hill48 model provides sufficient predictability of the directionality both in compressive yield stresses and R-values. The advantage of the non-AFR Hill48 model lies in that a more comprehensive consideration of the effect of anisotropy on deformations is correctly introduced.

Figure 5 compares the shape of plastic potential and yield function of Hill48 at zero vertical stress. It is observed that the potential function is much different from the yield surface and the non-AFR Hill48 yield function is accurate enough to describe the anisotropy in both the yield stress and plastic flow.

The stress-plastic strain curves are compared for the uniaxial compressions along different directions in Figure 6. The comparison obviously indicates that the compressive stress along the rolling direction is much larger than those along other directions. To be consistent with the yield stress at the vertical direction which is used for parameters identification above, the strain-hardening behavior at the vertical direction is incorporated into the user-defined material subroutine VUMAT. Unlike common exponential or power forms, there is a concave transition between yielding stress and the maximum compressive stress on each stress-plastic strain curve; thus in this paper a quintic polynomial is utilized to describe the strain-hardening behavior:

\[
\bar{\sigma} = 65360 \cdot \bar{\varepsilon}_p^3 + (-72170) \cdot \bar{\varepsilon}_p^4 + 29880 \cdot \bar{\varepsilon}_p^5 \\
+ (-5325) \cdot \bar{\varepsilon}_p^6 + 398.5 \cdot \bar{\varepsilon}_p + 52.27,
\]  

where \(\bar{\sigma}\) and \(\bar{\varepsilon}_p\) are the equivalent stress and the equivalent plastic strain, respectively. The coefficients in (17) are calibrated by experimental stress-plastic strain curve from uniaxial compression test along the vertical direction.

4. Numerical Integration Algorithm

Finite element implementation of the constitutive model requires numerical integration of the constitutive equations over the time increment. Here the semi-implicit backward Euler method proposed by Moran et al. [18] is adopted. The dominant feature of the semi-implicit backward Euler method is that it is implicit in plasticity parameter and explicit in the plastic flow direction and plastic moduli. That means the increments in the plasticity parameter are calculated at the end of the step while the plastic flow direction and plastic moduli are calculated at the beginning of the step. To avoid drift from the yield surface, the yield condition is enforced at the end of the step. The integration scheme is summarized as follows [19].

1. Give the set \((\sigma_t, \varepsilon_t, \varepsilon_p^t)\) at time \(t\) and the strain increment \(\Delta \varepsilon_{t+\Delta t}\).

2. Suppose the strain increment at the current time step is purely elastic, a trial stress or an elastic predictor is calculated:

\[
\sigma_{t+\Delta t}^{\text{trial}} = \sigma_t + C : \Delta \varepsilon_{t+\Delta t}.
\]

3. Substitute \(\sigma_{t+\Delta t}^{\text{trial}}\) into (1) to check the yield condition:

\[
f_{t+\Delta t}^{\sigma_p} = f_y \left( \sigma_{t+\Delta t}^{\text{trial}}, \varepsilon_p^{t+\Delta t} \right).
\]

If \(f_{t+\Delta t}^{\sigma_p} \leq 0\), it means an elastic process; then \(\sigma_{t+\Delta t} = \sigma_{t+\Delta t}^{\text{trial}}, \varepsilon_p^{t+\Delta t} = \varepsilon_p^t\); else, the yield surface is expanded and the following plastic correction is needed.
Table 1: Directional compressive yield stress and Lankford coefficients of hot rolled AZ31.

<table>
<thead>
<tr>
<th>Direction</th>
<th>0</th>
<th>30</th>
<th>45</th>
<th>60</th>
<th>90</th>
<th>Vertical</th>
</tr>
</thead>
<tbody>
<tr>
<td>Yield stress</td>
<td>61.29</td>
<td>61.96</td>
<td>63.89</td>
<td>66.56</td>
<td>87.46</td>
<td>63.43</td>
</tr>
<tr>
<td>R-value</td>
<td>0.4910</td>
<td>0.5087</td>
<td>0.5256</td>
<td>0.5385</td>
<td>0.5613</td>
<td>1.4401</td>
</tr>
</tbody>
</table>

Table 2: Material parameters in the Hill48 yield function for hot rolled AZ31.

<table>
<thead>
<tr>
<th>$F_Y$</th>
<th>$G_Y$</th>
<th>$H_Y$</th>
<th>$L_Y$</th>
<th>$M_Y$</th>
<th>$N_Y$</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.2275</td>
<td>0.7725</td>
<td>0.2985</td>
<td>1.4713</td>
<td>1.4713</td>
<td>1.4713</td>
</tr>
</tbody>
</table>

Table 3: Material parameters in the Hill48 plastic potential function for hot rolled AZ31.

<table>
<thead>
<tr>
<th>$F_P$</th>
<th>$G_P$</th>
<th>$H_P$</th>
<th>$L_P$</th>
<th>$M_P$</th>
<th>$N_P$</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.4666</td>
<td>0.5334</td>
<td>0.2619</td>
<td>1.0256</td>
<td>1.0256</td>
<td>1.0256</td>
</tr>
</tbody>
</table>

(4) Plastic correction:

(a) Initialization: set the initial equivalent plastic strain to the converged values at the end of previous time-step, zero the increment in plasticity parameter $\lambda$, and evaluate the elastic trial stress:

$$
k = 0 : \varepsilon^{(0)} = \varepsilon^{p(0)} , \quad \Delta \lambda^{(0)} = 0 ,
\sigma^{(0)} = \sigma_{trial} - \Delta \lambda^{(0)} C : r_t,
$$

where $r = \frac{\partial f_p}{\partial \sigma}$ represents the plastic flow direction and $\Delta \lambda^{(0)} C : r_t$ is the plastic corrector.

(b) Check yield condition and convergence at the $k^{th}$ iteration:

$$
f_y^{(k)} = f_y \left( \sigma^{(k)}, \varepsilon^{p(k)} \right).
$$

If $f_y^{(k)} < TOL$, converged, return (1); else, go to (c).

(c) Compute the increment in plasticity parameter:

$$
\delta \lambda^{(k)} = \frac{f^{(k)}}{\partial f^{(k)} : A^{(k)} : \tilde{r}_t},
$$

where

$$
[A^{(k)}] = \begin{bmatrix} C & 0 \\ 0 & -1 \end{bmatrix}, \quad \{ \tilde{r}_t \} = \begin{bmatrix} r_t \\ 1 \end{bmatrix},
$$

$$
[\partial f^{(k)}] = \begin{bmatrix} \frac{\partial f^{(k)}}{\partial \sigma^{ij}} \\ \frac{\partial f^{(k)}}{\partial \varepsilon^{i}} \end{bmatrix}.
$$

(d) Obtain the increments in stress and equivalent plastic strain:

$$
\begin{cases}
\Delta \sigma^{(k)} = -\delta \lambda^{(k)} [A^{(k)}] \{ \tilde{r}_t \}, \\
\Delta \varepsilon^{(k)} = -\delta \lambda^{(k)} [A^{(k)}] \{ \tilde{r}_t \}.
\end{cases}
$$

(e) Update the stress and equivalent plastic strain:

$$
\varepsilon^{p(k+1)} = \varepsilon^{p(k)} + \Delta \varepsilon^{p(k)},
\Delta \lambda^{(k+1)} = \Delta \lambda^{(k)} + \delta \lambda^{(k)},
\sigma^{(k+1)} = \sigma^{(k)} + \Delta \sigma^{(k)}.
$$

If $k \leftarrow k + 1$, go to (b).

The experimental and simulated deformations of the sample after uniaxial compression are compared in Figure 7 to validate the anisotropic constitutive model built according to the above theories and identified parameters. The Hill48 yield function under AFR is also used to simulate these deformation processes for the comparison purpose. It is obvious that the dimensions of all the three directional samples simulated by the non-AFR Hill48 model are in much better agreement with the experimental data than those predicted by the Hill48 yield function under AFR.

5. Application to the Hot Rolling Simulation

5.1. Square-Bar Rolling Pass. The calibrated Hill48 yield function under non-AFR is applied to simulate the elastoplastic deformation of AZ31 magnesium alloy during hot rolling process. For the comparison purpose, the von Mises yield function and the Hill48 yield function under AFR are also used in the simulation of square-bar hot rolling process.
shown in Figure 8, the square-bar billet with a cross-section of 20 mm × 20 mm is rolled by a thickness reduction of 40%. The elastic modulus of AZ31 is 44.9 GPa while the roller is assumed to be rigid. Rolling velocity is set to 1 m/s.

For simulation results predicted by both the isotropic and anisotropic material models, the feeding end of the billet is warped to some degrees as a result of initial interaction with the roller. However, it has little effect on the flatness of the remainder part. Besides, the lateral displacement near both ends is larger than that at the middle of the billet as depicted in Figure 9. Thus, the contour at the middle of the billet after rolling in Figure 9 is extracted from simulations with three plasticity models as compared in Figure 10. The comparison apparently reveals that the lateral spread at the middle of the billet is strongly affected by anisotropy of the material. It is observed that the lateral spread at the middle of the billet is 21% for the isotropic von Mises model, 39.9% for the AFR Hill48 function, and for the non-AFR Hill48 model the predicted lateral spread is 28.7%, which is between those predicted by the von Mises and Hill48 under AFR models.

5.2. Strip Rolling Pass. Simulations and experiments of a strip rolling pass are carried out to evaluate the predictability of
the non-AFR Hill48 model in predicting lateral spread. The rolling is operated on a reversible four-roller hot rolling mill for magnesium alloy plates. The hot rolling mill consists of two symmetrically arranged backup rollers and two working rollers as illustrated in Figure 11 (left). The billet thickness in experiments is identical with that of compression specimens so that the calibrated yield function in Section 3 can be utilized directly in simulation of strip rolling pass. The finite element model is described in Figure 11 (right) for an AZ31 strip billet with the 12 mm × 100 mm cross-section.

The experimental section at the middle of the deformed billet is compared with those predicted by the isotropic von Mises yield function, the Hill48 yield function under AFR, and the non-AFR Hill48 yield in Figure 12. The comparison demonstrates that the lateral spread of strips is severely underestimated by the isotropic von Mises yield function, while the Hill48 yield function under AFR overestimates the lateral spread. The Hill48 yield function under non-AFR predicts the lateral spread of the strip after rolling with very high accuracy.

6. Conclusions

The Hill48 yield function is combined with a non-AFR in a Hill48 form to describe the plastic behavior of AZ31 magnesium alloy. The non-AFR Hill48 yield function is calibrated by uniaxial compression tests since the proposed plasticity model is applied to hot rolling process during which materials mainly experience compression. The calibrated non-AFR Hill48 yield function was implemented in a user-defined material subroutine of ABAQUS/Explicit based on a semi-implicit backward Euler method. The user subroutine is utilized to simulate plastic deformation of uniaxial compression tests to verify the correct implementation of the non-AFR Hill48 yield function. The implemented non-AFR Hill48 yield function is utilized to simulate both square-bar rolling pass and strip rolling pass. The simulated lateral spreads are compared with experimental results and those predicted by the von Mises yield function and the Hill48 yield function under AFR. The comparison validates that the non-AFR Hill48 yield function calibrated by uniaxial compression tests can accurately model the plastic behavior of AZ31 magnesium alloy in hot rolling processes. Hence, the proposed non-AFR Hill48 yield function is suggested to be calibrated by the uniaxial compression tests for the accurate simulation of various rolling processes in design of rolling tools and factor optimization in rolling.
Figure 11: The four-roller hot rolling mill for magnesium alloys and the FE model for strip rolling.

Figure 12: Comparison of the cross-section profiles at the middle of the rolled strip billet.

Conflict of Interests

The authors declare that there is no conflict of interests regarding the publication of this paper.

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