



1 Article

2 Control-Oriented Modeling of a 3D Printed Soft

3 Actuator

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13 Abstract: A new type of soft actuator was developed by using hydrogel materials and 3D printing 14 technology, attracting the attention of researchers, particularly in soft robotics field. Due to 15 parametric uncertainties of such actuators, which originate in both custom design nature of 3D 16 printing as well as time and voltage variant characteristics of polyelectrolyte actuators, a 17 sophisticated model to estimate their behaviour is required. This paper presents a practical 18 modeling approach for the deflection of a 3D printed soft actuator. The suggested model is 19 composed of electrical and mechanical dynamic models that the earlier describes the actuator as a 20 resistive-capacitive (RC) circuit, whereas the latter model relates the ionic charges to the bending of 21 actuator. The experimental results were acquired to estimate the transfer function parameters of the 22 developed model incorporating T-S fuzzy sets. The proposed model was successful in estimation of 23 the end-point trajectory of the actuator especially in response to a broad range of input voltage 24 variation. With some modifications in the electromechanical aspects of the model, the proposed 25 modelling method can be used to other 3D printed soft actuators.

- 26 Keywords: Modeling; soft actuator; soft robot; 3D print
- 27

28 Introduction

29 In contrast to building robots from rigid materials in conventional robotics, soft, responsive, 30 flexible and compliant materials have been used to make composite materials that can mimic 31 biological systems. The study of such responsive composites is often referred to as soft robotics, 32 which is a specific category of the field of robotics. There has been a growing interest in these 33 materials which has potential applications in sensors and actuators. Functional components 34 composed of soft and active materials can be 3D printed. Further, it was observed that monolithic 35 structures independent of pneumatics or fluidics systems, which have their own shortcomings [1], 36 can be developed as muscle like actuators by means of materials like shape memory alloys, shape 37 memory polymers, or responsive hydrogel materials [1-3].

Using 3D bioprinting as part of fabrication of soft actuators from responsive materials such as hydrogel actuators with multi-material compositions with spatial control in interesting architectures has recently been investigated [4]. In a recent study polyelectrolyte chitosan hydrogel was used in the 3D printing of a soft actuator [5]. Chitosan has been found as an appropriate material for drug release, cell manipulation, and alike bio applications where the actuation and responsiveness to external stimuli is essential [6]. This has been mainly referred to its antibacterial properties which are attributed to free amino groups on the hydrogel backbone. 45 From one point of view hydrogels can be divided into two groups in terms of responsive 46 behaviour to potential gradient. A group known as non-ionic hydrogels do not demonstrate a notable 47 actuation response to input voltage when immersed in electrolyte solutions due to even distribution 48 of hydrated ions on two sides of hydrogels. Polyelectrolyte hydrogels, however, react differently 49 from non-ionic hydrogels when immersed into electrolyte solutions. Upon immersion in electrolyte 50 solutions and applying voltages, polyelectrolyte hydrogels show actuation behaviour based on 51 parameters like strength and polarity of input voltages and pH of solutions [7]. Various key factors, 52 such as ionic charge and crosslinking densities as well as polymer and external electrolyte 53 concentrations [7], have been identified to affect the amount of bending of polyelectrolyte hydrogels 54 in response to an input voltage. For chitosan hydrogel when is immersed into an electrolyte solution 55 with high pH, the carboxylic group would be deprotonated so as the hydrogel actuator take a 56 negative charge. Then, upon the application of voltage potentials on electrodes, the hydrated cations 57 enter to one side of the actuator more than other side. This result in an ionic strength difference 58 between inside and outside of the hydrogel leading to a greater osmotic pressure on one side of 59 hydrogel than the other side which in turn lead to bending of hydrogel actuator to the counter 60 electrode or cathode. Thus, the gel near the anode swells, causing it to bend toward the cathode [8]. 61 Noting that, along with osmotic pressure gradient, the ionic strength also affects the extent of bending 62 of the polyelectrolyte soft actuator. While because of higher electric voltage the movements of ions 63 are accelerated which lead to faster ionic and osmotic pressure gradients and therefore increase of 64 both bending angle and bending rate of the actuator. Yet, the relation of bending behaviour of the 65 actuator is not always proportional to ionic strength of electrolyte solution because of the shielding 66 effect phenomenon [9].

67 Polyelectrolyte soft actuators have been considered as an electro-chemo-mechanical system that 68 make their modeling quite complicated. The bending and actuation performances of polyelectrolyte 69 soft actuators are influenced by uncertainties and time-varying parameters stemming from back 70 relaxation and modulus variation phenomena. These undesirable factors should be dealt with for 71 further fabrication and applications of such soft actuators. However, with incorporation of 3D 72 printing in manufacturing of such soft actuators developing a control-oriented model for estimating 73 the behaviour of these 3D printed polyelectrolyte soft actuators in real world application are 74 demanded.

75 There have been studies on dynamics modelling of conventional polyelectrolyte soft actuators. 76 Black-box models were used in some works for calculating the curvature of the actuator based on 77 input voltage but were not scalable and too simple to describe the actuator performance entirely [10]. 78 Advanced gray-box models based on electrical circuit models, like RC [11] and distributed 79 transmission line models [12], have also been developed to correlate the applied voltage to the 80 bending of the actuators [13]. More complex white-box models [10-12] considering complicated 81 electro-chemo-mechanical principals have been developed to explain the more insightful details of 82 underlying physics for accurate dynamics modeling of the polyelectrolyte actuators. Yet, these 83 models realized too complex and not appropriate for real time control application of such actuators. 84 This study establishes a mathematical gray-box relation of the 3D printed polyelectrolyte soft actuator 85 by coupling both mechanical and electrical dynamics of the actuators.

Takagi-Sugeno (T-S) fuzzy modeling has been a practical approach in control designs applications [14], [15]. This study develops a reliable model of the 3D printed polyelectrolyte soft actuator based on the T-S fuzzy modeling strategy. The proposed model relates the different input voltages applied to the actuator to the bending of actuator via a universal T-S model surfing among the voltage dependent sub-models. This provides a scalable and practical model for further control applications of such systems.

92 The rest of paper is comprised of the following sections. First, 3D printing of the polyelectrolyte 93 soft actuator using chitosan is explained. Then, an electro-chemo-mechanical modeling of 3D printed 94 polyelectrolyte actuator is developed. Finally, the developed model is validated via the experimental 95 tests data.

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97 Fabrication of the Polyelectrolyte Actuator

98 Like other 3D print products, first, the actuator model was drawn in Solidworks (Dassault 99 Systemes, USA) and then the model was imported into an EnvisionTEC GmbH Bioplotter software 100 (EnvisionTEC, Gladbeck, Germany). The required materials including medium molecular weight 101 chitosan (with 75-85% deacetylation degree) and acetic acid solution were purchased from 102 SigmaAldrich, Australia. A mixture of 1.6 g chitosan in 0.8 ml acetic acid solution (1 v/v%) was made 103 under vigorous stirring at 50°C, for 2 h. The resultant 3D print ink was then prepared through 104 sonication and centrifugation. Finally, the ready to print ink was poured into a low-temperature 3D 105 Bioplotter syringe. For solidifying each layer after extrusion, a solution of Ethanolic Sodium 106 Hydroxide (EtOH-NaOH) with 0.25 M NaOH (Sigma Aldrich), 70 v/v% EtOH (3:7 ratio), was 107 prepared. The porous chitosan beam with the size of 40 mm by 8 mm by 2 mm was printed layer by 108 layer (Fig. 1(a)). The 3D printing was performed with optimized parameters of 3D Bioplotter as 109 explained extensively in an earlier work of authors [16].

110 Electro-Chemo-Mechanical Model of the 3D Printed Polyelectrolyte Actuator

111 To circumvent the complexity of Multiphysics modeling, this study suggests a scalable model

- 112 of the polyelectrolyte actuator. Doing so, various factors are considered in the behavior of the
- 113 actuators to estimate the dynamics parameters more realistically. Thus, the actuator model comprises
- 114 both electrochemical and electromechanical models considering their dynamics coupling.



115

Figure 1. (a) An arbitrary pattern 3D printed polyelectrolyte actuator; (b) different patterns and sizes of 3D printed polyelectrolyte actuators.

118 Electrochemical Modelling

| 119 | An electrochemical RC model that gives the relation between applied voltage and current flown |
|-----|--|
| 120 | across the polyelectrolyte gel is illustrated in Fig. 2. A diffusion model to represent the current flow |
| 121 | across the 3D printed polyelectrolyte actuator are calculated from the Fick's law of diffusion as: |

$$i_D(t) = -F \times A \times D \times \frac{\partial c(y,t)}{\partial y},\tag{1}$$

122 where (*c*) refers to the ion concentration, the path along the thickness of the actuator is indicated by 123 y, (*D*) is the diffusion coefficient constant, (*A*) is the area between the interface of electrolyte solution 124 and polyelectrolyte actuator, and (*F*) denotes the Faraday constant. Then, the current running across 125 the double layer capacitance can be calculated assuming the double-layer capacitance thickness as 126 (δ):

$$i_{c}(t) = F \times A \times \delta \times \frac{\partial c(y,t)}{\partial y}.$$
(2)

127 Next, for a 3D printed polyelectrolyte actuator with the thickness of the (*h*), the diffusion 128 equation model can be written as:

$$\frac{\partial c(y,t)}{\partial t} = D \frac{\partial^2 c(y,t)}{\partial y^2} \quad 0 < y < h, \ \frac{\partial c(y,t)}{\partial t} (@y = h) = 0.$$
(3)



129

Figure 2. Equivalent RC circuit where (Z_d) is the diffusion impedance, (C_{dl}) denotes the double layer capacitance, and (R_s) refers to the resistance the electrolyte solution.

Finally, an electrochemical model relating the current flown across the actuator to the appliedvoltage can be obtained by simultaneous solving the Eqs. 1-3 as:

$$\frac{I(s)}{V(s)} = \frac{s\left[\frac{\sqrt{D}}{\delta}\tanh\left(h\sqrt{\frac{s}{D}}\right) + \sqrt{s}\right]}{\frac{\sqrt{s}}{c_{dl}} + s\sqrt{s}R_s + R_s\frac{\sqrt{D}}{\delta}s\tanh\left(h\sqrt{\frac{s}{D}}\right)}.$$
(4)

134 *Electromechanical Modelling*

135 An electromechanical model that relates the osmotic pressure caused by input voltage to the 136 bending of 3D printed polyelectrolyte actuator is developed in this section. Assuming the strain-to-137 charge ratio α , the relation between the charges density (ρ_{ch}) and resulted in-plane strain (ε) in 138 polyelectrolyte actuators can be written as [18]:

$$\varepsilon = \alpha \rho_{ch} , \qquad (5)$$

139 where for a 3D printed soft actuator with size of (*W*) and (*L*) as width and length respectively, (ρ_{ch}) 140 can be calculated as:

$$\rho_{ch} = \frac{1}{WLh} \int_0^t I(t) dt \xrightarrow{L} \rho_{ch}(s) = \frac{I(s)}{sWLh}, \tag{6}$$

141 Generally, actuators strains are calculated knowing the tip displacement, initial length and 142 thickness of the actuators when the bending curvature is comparatively small. But, the curvature 143 radius is not negligible when the soft actuators experience larger bending. In this study, as shown in 144 Fig. 3 and Eq. 7, the strain (ε) resulted purely from bending of the actuator is obtained as:

$$\varepsilon = \frac{l_o - l_c}{l_c} = \frac{(R + y)\theta - R\theta}{R\theta} = \frac{y_b}{R} = Ky_b , \qquad (7)$$

145 where (l_o) and (l_c) are the swelled length and the centered length of actuators, (θ) and (R) refer to 146 the bending angle and the radius of curvature of the actuator respectively, (y_b) shows the distance 147 between the outer edge of swelled layer and the reference plane, and (K) is the bending curvature of 148 the actuator. To estimate an accurate value of the stress induced on the bending of actuator the 149 superposition of actuations effect and the bending strain are considered together, so, the total induced

- 150 stress, assuming the Young's modulus of the 3D printed polyelectrolyte actuator as (E), can be
- 151 calculated as follows:

$$\sigma = E(K \mp \alpha \rho_{ch}),\tag{8}$$

152 where the opposite signs representing the expansion and contraction of sides of actuators.



153 154

Figure 3. Schematic of the bending of the printed actuator.

155 Equaling the total moments and forces on the actuators to zero, the bending curvature (K) can 156 be realized. This is somehow related to a new defined coefficient φ as follows:

$$\sum F = \int_{-h/2}^{0} E(Ky_b + \alpha \rho_{ch}) y_b dy_b + \int_{0}^{h/2} E(Ky_b - \alpha \rho_{ch}) y_b dy_b = 0,$$

$$\sum \sigma = \int_{-h/2}^{0} E(Ky_b + \alpha \rho_{ch}) dy_b + \int_{0}^{h/2} E(Ky_b - \alpha \rho_{ch}) dy_b = 0,$$

$$K = \varphi \rho_{ch}, \text{ where } \varphi = \frac{3\alpha}{Eh}.$$
(9)

157 Combining Eqs. 9 and 6 into Eq. 4, bending curvature can be expressed as:

$$K(s) = \frac{\varphi V(s)}{WLh} \frac{\left[\frac{\sqrt{D}}{\delta} \tanh\left(h\sqrt{\frac{s}{D}}\right) + \sqrt{s}\right]}{\frac{\sqrt{s}}{C_{dl}} + R_s s\sqrt{s} + R_s \frac{\sqrt{D}}{\delta} s \tanh\left(h\sqrt{\frac{s}{D}}\right)}.$$
(10)

158 Finally, the model relating the applied voltage to bending of the 3D printed polyelectrolyte 159 actuator can be obtained by incorporating Eq. 6 and Eqs. 5-10 as following [19]:

$$\frac{Y(s)}{V(s)} = \frac{\varphi}{WLh} \frac{1}{sR_s + \frac{1}{C_{dl} \left[1 + \frac{\sqrt{D}}{\delta\sqrt{s}} \tanh\left(h\sqrt{\frac{s}{D}}\right)\right]}}, \text{ where, } Y(s) = \frac{1}{K(s)} \mp \sqrt{\frac{1}{K(s)^2} - L^2}.$$
(11)

- 160 The Eq. 11 needs to be restructured to be practical for control applications due to presence of hyperbolic tangent term in its denominator leading to be dimensionally infinite. To deal with this, 161 162 the dimensionally infinite hyperbolic tangent term can be replaced by Mittag Leffler's expansion as:

r—

$$\frac{\tanh(\frac{1}{2}\sqrt{\frac{X}{Y}})}{4\sqrt{XY}} = \sum_{n=0}^{\infty} \frac{1}{X + n^2((2n+1)^2Y)'},$$
(12)

163 where X = s, and $Y = D/4h^2$. This simplification confines the model in a bounded range of 164 frequencies for input voltages within the interest low frequency range for the 3D printed 165 polyelectrolyte soft actuator. Hence, Eq. 12 represents the model for the small values of (n), so as a 166 fourth order model approximates bending displacement of the 3D printed soft actuator as:

$$\frac{Y(s)}{V(s)} = e^{\beta s} \frac{(s+z_1)(s+z_2)(s+z_3)}{(s+p_1)(s+p_2)(s+p_3)(s+p_4)'}$$
(13)

167 where β is a real value and zi's (*n*=1,2,3) are the zeros and pi's (*n*=1,2,3,4) are the poles of the soft 168 actuator transfer function.

- 169 T-S Fuzzy System Modeling Formulation
- 170 Consider a simplified dynamic system without uncertainties systems as:

$$\dot{x} = A(x) + B(x)u. \tag{14}$$

- 171 Fuzzy inference rules for T-S fuzzy dynamic model of Eq. 16 can be described as follows [20]:
- 172 R^i : IF z_1 is w_1^i AND ... z_n is w_n^i

$$\dot{x} = A^{i}(x) + B^{i}(x)u$$
 for $i = 1, ..., m$, (15)

- where the matrices $A^i \in \mathbb{R}^{n \times n}$ and $B^i \in \mathbb{R}^{n \times 1}$ represents the subsystem parameters, $z = (z_1, ..., z_n)^T$, 174 175 behavior. x is system state variable vector and u is the system input. R^i represents the i^{th} fuzzy 176 inference rule, $z(t) = [z_1(t) z_2(t) \dots z_n(t)]$ among *m* number of inference rules.
- 177 Knowing M_i (j = 1, ..., n) are the fuzzy sets, the inferred fuzzy set w^i can be used to calculate μ_i as
- 178 the normalized fuzzy membership function of inferred fuzzy sets as follows:

.

$$w^{i} = \prod_{j=1}^{n} M_{j}^{i}, \qquad \mu^{i} = \frac{w^{i}}{\sum_{i=1}^{m} w^{i}}, and \sum_{i=1}^{m} \mu^{i} = 1.$$
 (16)

179 The singleton fuzzifier, product inference, and center-average defuzzifier are used to form the 180 global dynamic fuzzy model of the nominal system of Eq. 17 as:

$$\dot{x} = A(\mu)x + B(\mu)u(t),$$

$$A(\mu) = \sum_{i=1}^{m} \mu^{i} A^{i}, B(\mu) = \sum_{i=1}^{m} \mu^{i} B^{i}, \text{ where } \mu = (\mu^{1}, \mu^{2}, ..., \mu^{m}).$$
(17)

181 Actuator Characterization

182 The bending of the 3D printed polyelectrolyte hydrogel actuator can be justified by Donnan effect 183 phenomenon. This means that the motion of counterions initiated by applied voltage leads to the 184 ionic gradient within the hydrogel networks along the direction of the electric field. This results in an 185 osmotic pressure difference within the hydrogel structure, and consequently causes the deflection of 186 3D printed actuator toward the counter electrode. Several factors can be considered to characterize 187 the behaviour of the actuator. First, the effects of the electrolyte solution and its concentration on the 188 bending behaviour of the 3D printed polyelectrolyte actuator should be defined. Doing so, two 189 different electrolyte solutions, NaOH and NaCl, were opted to test the 3D printed actuator endpoint 190 deflection behaviour. The maximum endpoint deflection for the same sizes (40mm × 8mm × 2mm) 191 and patterns of 3D printed actuators are measured with respect to the ionic strength of the electrolyte 192 solutions. A constant voltage of 5 V was applied between the electrodes and the concentration of 193 NaOH and NaCl solutions were set in the range of [0.1, 0.2] M with increment of 0.2 M for each 194 experiment. The experiments repeated three times and results are depicted in Fig. 4(a). Regardless of 195 concentration of electrolyte solution, actuator has reached to more deflection in NaOH solution than 196 in NaCl solution. Also, it is observed that for both electrolyte solution there were an optimum value 197 for electrolyte ionic strength to achieve maximum bending angle. As shown in Fig. 4, this optimum 198 value for the 3D printed actuator tested here was nearby 0.12 M. It is seen that from 0.1 to 0.12 M the 199 endpoint deflection of the 3D printed actuator increased. This can be attributed to an increase of the 200 free ions moving from the surrounding solution toward their counter-electrodes. However, if the 201 concentration of the solutions were greater than the critical concentration, 0.12 M, the shielding effect 202 of the poly-ions occurred leading to a reduction in the electrostatic repulsion of the poly-ions, and 203 the subsequent decrease in the endpoint deflection. Hence, in the rest of paper all tests are performed 204 in NaOH electrolyte solution of 0.12 M.

205 Furthermore, several different patterns and dimensions of the actuators with the same material 206 are 3D printed (Fig. 1(b)). Then, the behaviour of the 3D printed actuators based on different 207 dimensions are investigated and the results are inserted in Table 1. The results reveal that the

208 maximum endpoint deflection of the actuators increase in proportion to their length while it shows 209 almost no correlation with the width of the actuator. It was also observed that the bending deflection 210 was inversely correlated to the thickness of the actuator [4].

To reveal hysteresis behaviour of 3D printed actuator the repeatability tests were performed. The same pattern and size of 3D printed samples of actuators were excited with a square wave electrical stimulus. The magnitudes of the square waves were selected as 5 V with the period of 220 s and duty cycle of 50%. The duration of experiment was set to be 5 times of period, and the performances of the actuators were compared based on change in maximum magnitudes in each cycle as shown in Fig. 4(b). The results showed that all actuators reached their maximum deflections

at the first set of experiments for a specific excitation voltage.



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Figure 4. (a) Response of the actuators with same pattern and dimensions to different electrolyte
 solutions; (b) maximum endpoint deflections of the actuators to 5 V input signal over different cycles.
 Error bars indicate the standard deviation of the maximum distance measured over the three trials.

| Astrator | Length | Width | Thickness | Maximum |
|----------|--------|-------|-----------|-----------------|
| Actuator | (mm) | (mm) | (mm) | deflection (mm) |
| S1 | 40 | 8 | 2 | 5.92 |
| S2 | 40 | 8 | 1 | 8.27 |
| S3 | 40 | 4 | 2 | 5.38 |
| S4 | 20 | 8 | 2 | 1.83 |

222 Table 1. Results of maximum endpoint deflection for same pattern and different sizes of 3D printed actuators.

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In next stage, actuator's endpoint deflections were tested overtime based on different input voltage magnitudes as illustrated in Fig. 5. From the results, it can be deduced that the actuation performance increased in the higher voltage; however, the occurrence of electrolyses and bubbling in electrolyte caused undesirable effects and limit application of higher voltages in such actuators.

Actuator responses under various frequencies were also investigated. Square voltage of 5V was applied between two electrodes in various frequencies, 0.0025, 0.02, 0.031, 0.054, 0.11, 0.15, and 1.1 Hz. It can be seen from figures 6(a) that the maximum endpoint deflections decrease with increasing frequency since the actuators have less time to respond. Also, response time to the first peak were measured and were demonstrated in figure 6(b). From the figure can be observed that the actuator reaches the first peak faster as the magnitude of the peaks decrease in higher frequencies.



234 235 236

Figure 5. (a) Response of the actuators with same pattern and dimensions to (b) different input voltages' magnitudes. The results are averaged over the three trials.



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Figure 6. (a) Response of actuator's maximum endpoint deflection to various frequencies under 5 V
 square waves; (b) response time to first peak. Error bars indicate the standard deviation of the
 maximum distance measured over the three trials.

241 Modelling and Experimental Results

Now Golubev method [21] is used to estimate an appropriate model for control of actuator [22243 25]. Using Golubev method for the input signal, the uncertain transfer function relating the applied
voltage to the bending angle of the actuator is estimated as:

$$G(s) = e^{\beta s} \frac{a_1 s^3 + a_2 s^2 + a_3 s + a_4}{b_1 s^4 + b_2 s^3 + b_3 s^2 + b_4 s + b_5},$$
(18)

The frequency response model of the actuators with different patterns and sizes, shown in Fig. 1(b), are identified based on Eq. (18) and the experimental data are depicted in Fig. 7. It is observed that changing various parameters of the actuator, like different sizes and patterns, lead to a new set of linear voltage dependent transfer functions. Therefore, for each specific actuator a system identification of frequency response to different voltage levels are required. Then, T-S fuzzy model should be incorporated to interrelate the linear transfer functions at different voltage levels for improving the model accuracy.



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Figure 7. Frequency response system identification of different 3D printed actuators in response to
 5V input signal.

To identify transfer function parameters for the arbitrary pattern actuator S1, lower and upper limit input signals, 2V (shown in Fig. 8a) and 8V are applied to the system and the range of parameters identified as follows:

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259 $a_1 \in [0.0063, 0.0085]; a_2 \in [0.6381, 0.842]; a_3 \in [1.152, 1.924]; a_4 \in [1.14, 1.97];$

260 $b_1 \in [1,1]; b_2 \in [0.3631, 0.5898]; b_3 \in [225.5, 367.2]; b_4 \in [14.98, 29.41]; b_5 \in [0.2142, 0.2275];$ 261 $\beta = -3.67.$

262

263 Then, a two-rule based T-S model is defined as:

264 Rule 1: IF $|z(t)| \le 5$ THEN $\dot{x} = A_1 x(t) + B_1 u(t)$.

265 Rule 2: IF $5 < |z(t)| \le 8$ THEN $\dot{x} = A_2 x(t) + B_2 u(t)$.

Finally, the outputs of the T-S fuzzy model (shown in Fig. 7b) can be calculated as:

$$\dot{x} = \mu_1(z(t)) (A_1 x(t) + B_1 u(t)) + \mu_2(z(t)) (A_2 x(t) + B_2 u(t)),$$
(19)
where $\mu_1(z(t)) + \mu_2(z(t)) = 1.$

267 A comparison of experimental tests with the T–S fuzzy model and estimated specific voltage 268 models for 2V and 8V input signals is shown in Figs. 9 and 10. The data is the average of three 269 experiments to confirm reproducibility. Also, the efficacy of the developed model in terms of 270 scalability of the 3D printed soft actuators with different patterns and sizes are shown in Figs. 10(b) 271 and 10(c) where two actuators with arbitrary and lattice patterns and sizes S1 and S4 are compared 272 in response to an analogous input. These figures show supremacy of actuator end-point position 273 estimation by T-S fuzzy modelling compared to specific constant voltage models even with changing 274 the 3D printed actuator parameters such as pattern and size. Furthermore, looking at Fig. 10(b) in 275 detail reveals some discrepancy of the T-S model from experimental results, especially over longer 276 experimental tests. This is attributed to the time-varying intrinsic nature of the polyelectrolyte soft 277 actuator that demands feedback controller for compensation purpose in future study.



(a) (b) **Figure 8.** (a) An example of input signal for model identification (2v); (b) membership function of T-S model.

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Figure 10. (a) Input voltage signal; (b) endpoint deflection of arbitrary pattern actuator with size of S1; (b)
 endpoint deflection of lattice pattern actuator with size of S4.

290 Conclusion

291 A control-oriented modelling approach for 3D printed polyelectrolyte soft actuators was 292 presented in this study. First, 3D printed actuator with an arbitrary pattern was developed and 293 characterized based on different sizes, electrolyte concentration, input magnitudes, and frequencies. 294 Then, a linear transfer function of the 3D printed polyelectrolyte soft actuator was developed to 295 estimate the actuator behavior at different voltage signals. T-S fuzzy model was further employed for 296 better presentation of actuator model in a range of voltage variations via interrelating the voltage 297 dependent models. The experimental results showed improved performance obtained by using T-S 298 fuzzy model compared to linear transfer function at different voltages. The proposed model could be 299 used for other 3D printed soft actuators with custom design geometries due to its scalability.

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